

# **Intro to Statistics Formula Sheet**



#### A) Reminder:

**BEDM(S)AS** – Brackets, Exponents, Division, Multiplication, Sum ( $\Sigma$ ), Addition, Subtraction

#### B) Central Tendency (Ch. 3)

Population mean:  $\mu = \frac{\sum X}{N}$  Sample mean:  $M = \frac{\sum X}{n}$ 

## C) Sum of Squares (Ch. 4, p. 70-71)

Definitional Formula:  $SS = \sum (X - \mu)^2$ 

Computational Formula:  $SS = \sum X^2 - \frac{(\sum X)^2}{N}$ 

#### D) Variance (Ch. 4)

Definitional Formula:  $\sigma^2 = \frac{\sum (X - \overline{X})^2}{N}$ Computational Formula:  $\sigma^2 = \frac{\sum X^2 - \frac{(\sum X)^2}{N}}{N}$ Basic Formula:  $\sigma^2 = \frac{SS}{N}$ 

Definitional Formula:  $s^2 = \frac{\sum (X - \overline{X})^2}{n-1}$ Computational Formula:  $s^2 = \frac{\sum X^2 - \frac{(\sum X)^2}{n}}{n-1}$ Basic Formula:  $s^2 = \frac{SS}{n-1}$ 

#### E) Standard Deviation (Ch. 4)

#### F) z-Score (Ch. 5)

For locating an X value's position within a sample:

$$z = \frac{X - \mu}{\sigma}$$
  $X = z\sigma + \mu$   $\sigma = \frac{X - \mu}{z}$ 

For locating a sample mean's position within a population:

$$z = \frac{M - \mu}{\sigma_M}$$
  $M = z\sigma_M + \mu$   $\sigma_M = \frac{\sigma}{\sqrt{n}}$   $OR$   $\sigma_M = \sqrt{\frac{\sigma^2}{n}}$ 

#### **Finding Degrees of Freedom**

z-Scores	
Single Sample t-Statistic	df = n - 1
Paired / Related Sample t-Statistic	
Independent Samples t-Statistic	$df = (n_1 - 1) + (n_2 - 1)$
Paired Samples t-Statistics	$u_1 - (u_1 - 1) + (u_2 - 1)$
Independent Measures ANOVA:	$df = (df_{between}), (df_{within})$
	$df_{between} = k - 1$
	$df_{within} = N - k$
Repeated Measures ANOVA:	$df = (df_{between}), (df_{error})$
	$df_{between} = k - 1$
	$df_{error} = (N - K) - (n - 1)$
Chi-Square:	If single row of data: $df = C - 1$
	If table of data: $df = (R - 1)(C - 1)$



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G) Single Sample t-Statistic (Ch. 7)

$$t = \frac{M - \mu}{s_M}$$

$$t = \frac{M-\mu}{s_M}$$
  $s_M = \frac{s}{\sqrt{n}}$   $OR$   $s_M = \sqrt{\frac{s^2}{n}}$ 

H) Independent Measures & Two Samples t-Statistic (Ch. 8)

$$t = \frac{(M_1 - M_2) - (\mu_1 - \mu_2)}{s_{M_1 - M_2}}$$

If sample sizes are the same:  $s_{M_1-M_2} = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$ 

If the sample sizes are different:  $s_{M_1-M_2} = \sqrt{\frac{s_p^2}{n_1} + \frac{s_p^2}{n_2}}$ 

Pooled Variance:  $s_p^2 = \frac{ss_1 + ss_2}{df_1 + df_2}$ 

I) Paired Samples & Related Samples t-Statistic (Ch. 9)

$$t = \frac{M_D - \mu_D}{s_{M_D}} \qquad s_{M_D} = \frac{s_D}{\sqrt{n}}$$

J) Independent Measures & Repeated Measures ANOVA (Ch. 10)

$$SS_{total} = \Sigma X^{2} - \frac{G^{2}}{N}$$

$$SS_{between} = \Sigma \frac{T^{2}}{n} - \frac{G^{2}}{N}$$

$$df_{total} = N - 1$$

$$SS_{\text{between}} = \Sigma \frac{T^2}{n} - \frac{G^2}{N}$$

$$df_{between} = k - 1$$

 $SS_{within} = \Sigma SS_{within (each condition)}$ 

$$df_{within} = N - k$$

$$MS_{between} = \frac{SS_{between}}{df_{between}}$$

$$MS_{within} = \frac{SS_{within}}{df_{within}}$$

$$F = \frac{MS_{between}}{MS_{within}}$$

# K) Pearson Correlation (Ch. 11)

$$r = \frac{SP}{\sqrt{(SS_x)(SS_y)}}$$

$$SP = \Sigma XY - \frac{(\Sigma X)(\Sigma Y)}{n}$$

$$SS_x = \Sigma X^2 - \frac{(\Sigma X)^2}{n}$$

$$SS_y = \Sigma Y^2 - \frac{(\Sigma Y)^2}{n}$$

### L) Chi-Square Statistic (Ch. 12)

$$\chi^2 = \Sigma \frac{(f_o - f_e)^2}{f_e}$$

